

1. Consider a function

$$f(x) = \sqrt{x^2 - 4x + 3}$$

- (a) Find a domain of f (i.e., all x for which f is well defined).
- (b) Compute f' .
- (c) Find a domain of f' .
- (d) Compute f'' .

2. Integrals:

- Compute

$$\int \frac{1}{x-1} dx.$$

- Compute

$$\int \frac{1}{x^2 + 2x + 2} dx.$$

- Use the previous result in order to compute

$$\int \frac{x^2 + 5x + 9}{x^3 + x^2 - 2} dx.$$

3. Find all solutions to the equation

$$y' = y(100 - y).$$

Then, find a particular solution which fulfills $y(0) = 50$.

4. Consider an equation

$$y''' + y' = 3x$$

- (a) Find all solution to the appropriate homogeneous problem.
- (b) Use a 'special right hand side' method to deduce one particular solution.
- (c) Write all solutions to the given problem.