Second midterm test – sample, 12^{th} April 2024

Name:

Points: /25

1. Compute

$$\int x^5 \sin(x^3) \, \mathrm{d}x.$$

Points: /5

2. Compute

$$\int \frac{x+2}{(x-2)(x^2+4)} \, \mathrm{d}x.$$

Points: /5

3. Evaluate

$$\int_0^2 x^2 \sqrt{8 - x^3} \, \mathrm{d}x.$$

Points: /5

4. Write down the horizontal and vertical cross-section of the triangle M which has vertices (-1, -1), (0, 3) and (-1, 4).

Points: /5

5. Compute

$$\int x \, \mathrm{d}x \mathrm{d}y$$

over the set

$$M = \{(x, y) \in \mathbb{R}^2, 1 - x^2 \le y \le 3 - 3x^2\}.$$

Points: /5

Name:

Points: /25

1. Compute

$$\int x \log^4 x \, \mathrm{d}x.$$

Points: /5

2. Compute

$$\int \frac{x^3}{(x^2 - 4)} \, \mathrm{d}x.$$

Points: /5

3. Evaluate

$$\int_0^{\pi/2} \sin x \left(\cos^3 x + \cos x + 1\right) \, \mathrm{d}x.$$

Points: /5

4. Change the order of integration of

$$\int_0^1 \left(\int_{-2x^2}^{-x^2} f(x, y) \, \mathrm{d}y \right) \, \mathrm{d}x.$$

Points: /5

5. Compute

$$\int_{M} y \, \mathrm{d}x \mathrm{d}y$$

where M is the triangle with vertices (-2,0), (-2,6) and (1,3).

Points: /5